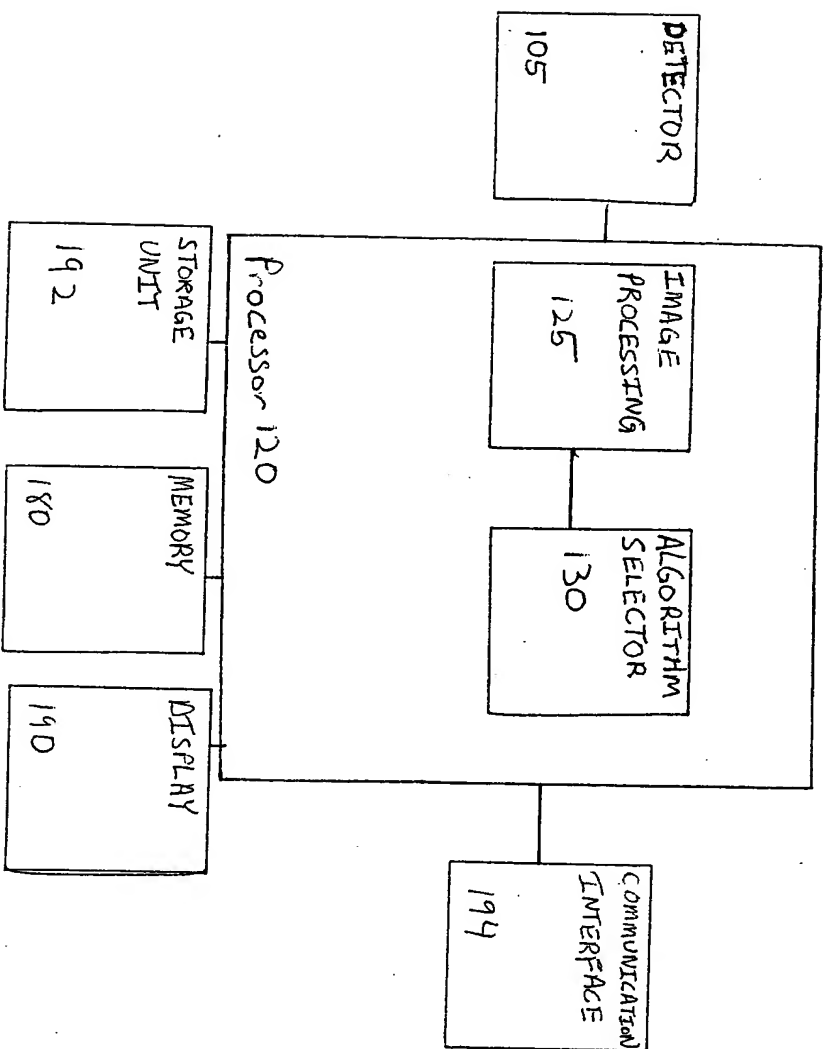


FIG 1



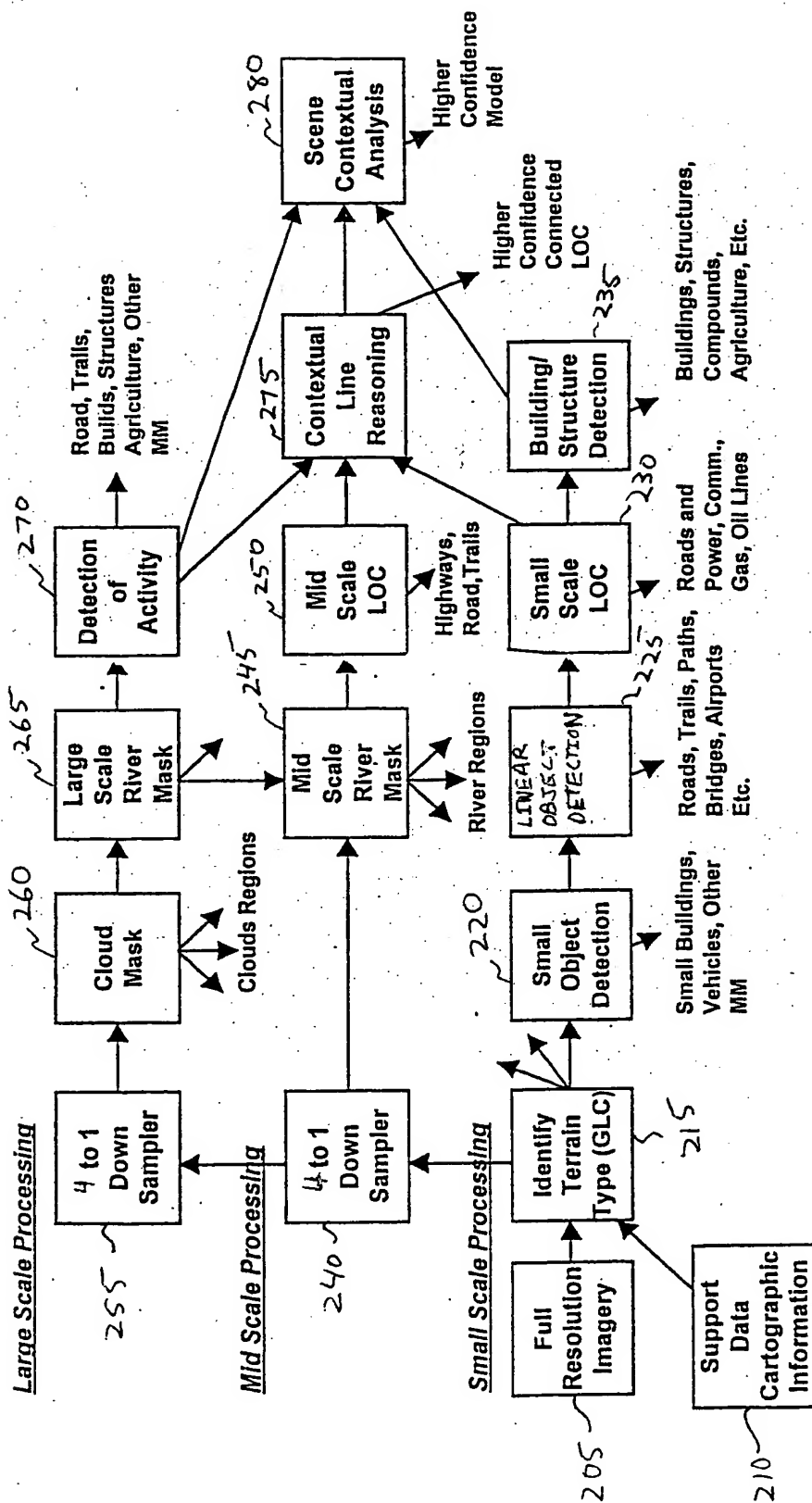


FIG 2

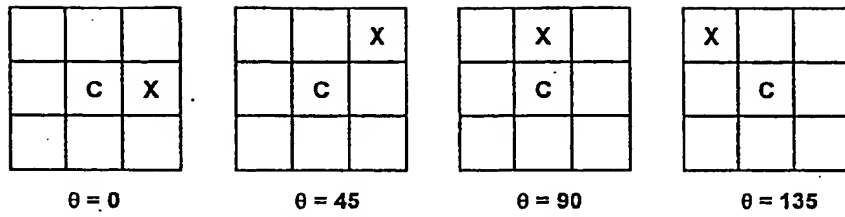


FIG 3

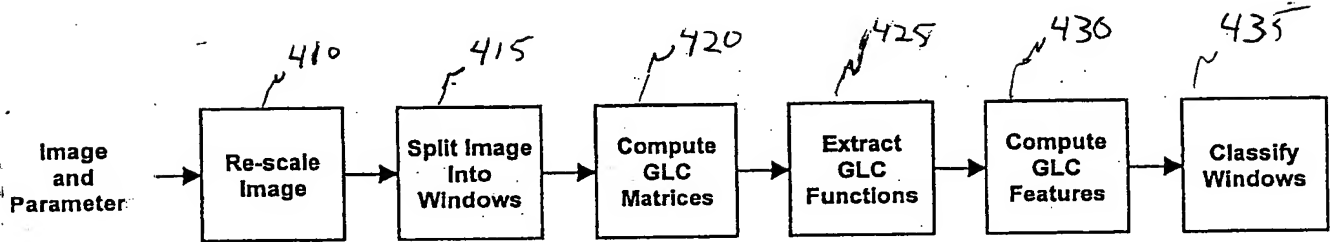


FIG 4

Energy

$$E_n = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} (G(i, j))^2$$

Entropy

$$E_t = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} (G(i, j) \log(G(i, j)))$$

Contrast

$$C_t = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} (G(i, j) \times (i - j)^2)$$

Inverse_Difference_Moment

$$E_n = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} \frac{G(i, j)}{1 + (i - j)^2}$$

Correlation

$$C_r = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} \frac{i \times j \times G(i, j) - \mu_x \times \mu_y}{\sigma_x \times \sigma_y}$$

FIG 5

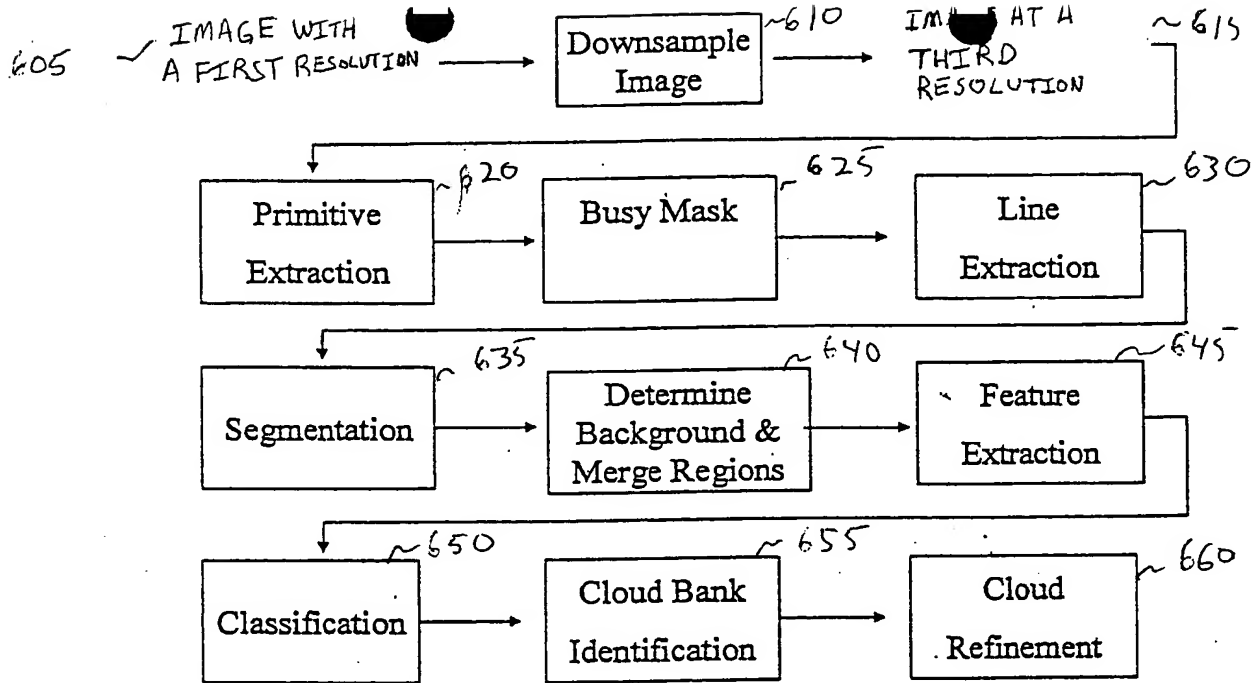
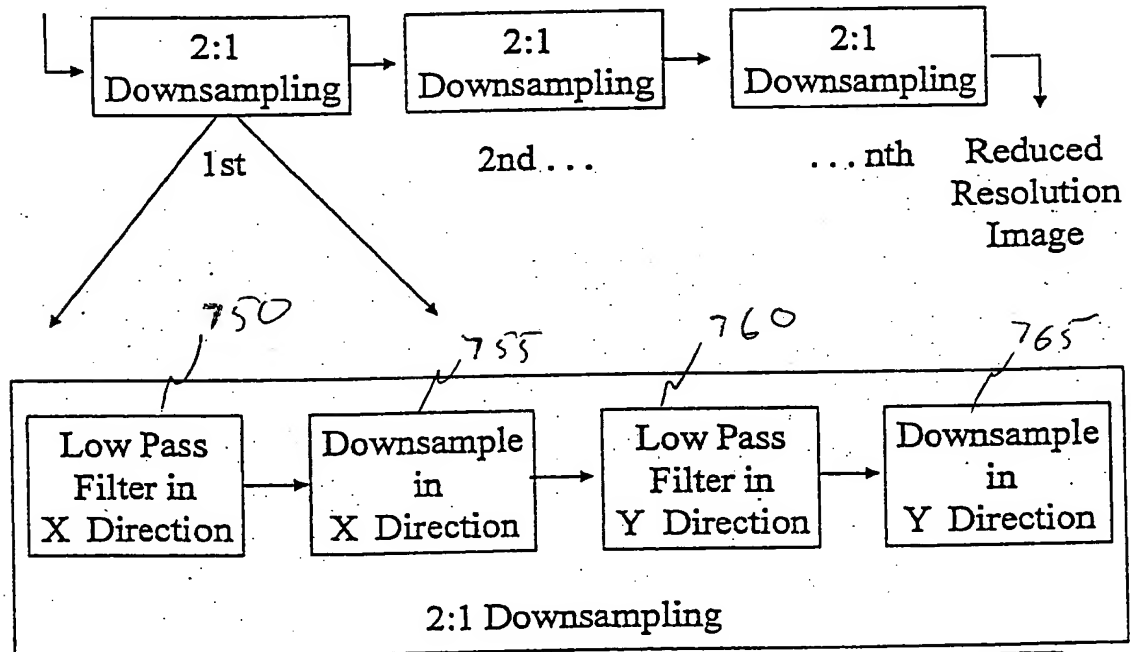


FIG 6

IMAGE WITH A FIRST RESOLUTION

FIG 7A



1	4	6	4	1
1	16	24	16	1
1	24	36	24	1
1	16	24	16	1
1	4	6	4	1

Full 6 by 6 Convolution Filter

FIG 7B

1	4	6	4	1
---	---	---	---	---

X Direction Filter

FIG 7C

1
4
6
4
1

Y Direction Filter

FIG 7D

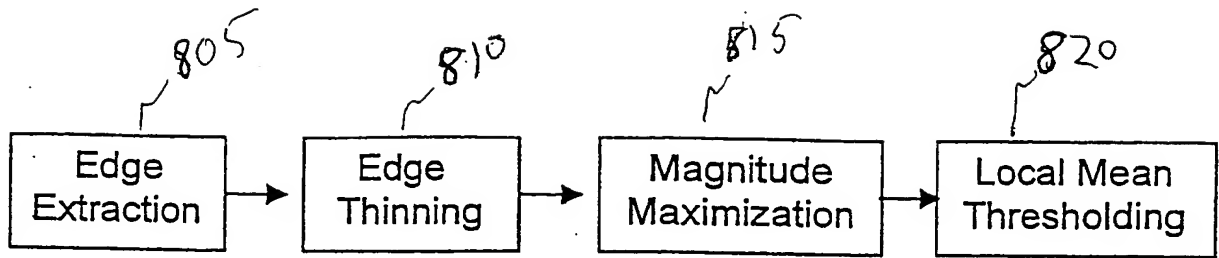


FIG 8

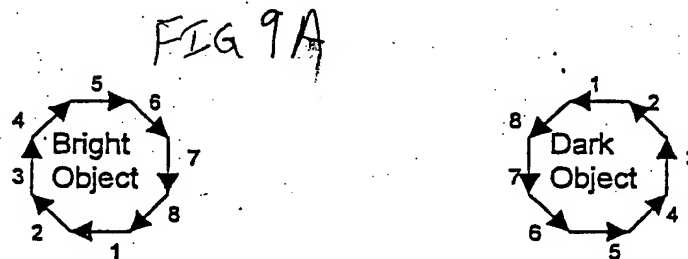
-1 -2 -1	-1 0 1	4 5 6
0 0 0	-2 0 2	3 * 7
1 2 1	-1 0 1	2 1 8
Horizontal Component Template	Vertical Component Template	Directional Mapping

D_x = convolution of the vertical template with the image

D_y = convolution of the horizontal template with the image

$$\text{Sobel Magnitude} = (D_x^2 + D_y^2)^{1/2}$$

Sobel Direction = $\text{Arctan} (D_y / D_x)$ mapped to 8 directions



<u>Directions 3 & 7</u>	<u>Directions 1 & 5</u>	<u>Directions 2 & 6</u>	<u>Directions 4 & 8</u>
O O O O O	O X X X O	O O O X O	O X O O O
X O O O X	O O X O O	O O O X X	X X O O O
X X C X X	O O C O O	O O C O O	O O C O O
X O O O X	O O X O O	X X O O O	O O O X X
O O O O O	O X X X O	O X O O O	O O O X O

C = Center pixel X = Non-zero pixel O = Don't care pixel

FIG 10

```

      XXX
     XXXXX
    XXXXXX
   XXXXXX
  XXXXXX
 XXXXX
XXXX

```

FIG 11A

```

      XXX
     XXX
    XXX
   XXX
  XXX
 XXX
XX

```

FIG 11B

X1X	X1X	XXO	OXX
XC1	1CX	1CX	XC1
OXX	XXO	X1X	X1X

1 = non-zero pixel, o = zero pixel, x = don't care

FIG 12

```

      XXX
     XXX
    XXX
   XXX
  XXX
 XXX
XX

```

FIG 13A

```

      XX
     XX
    XX
   XX
  XX
 XX
XX

```

FIG 13B

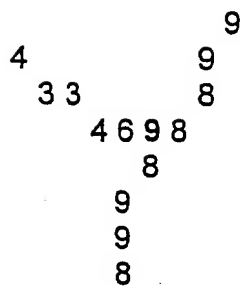


FIG 14A

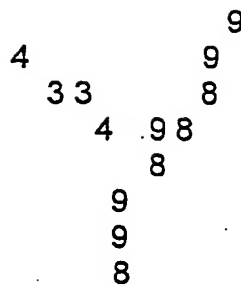


FIG 14B

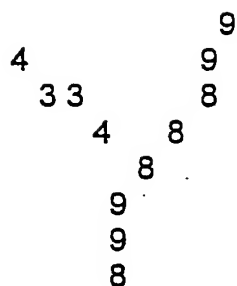


FIG 14C

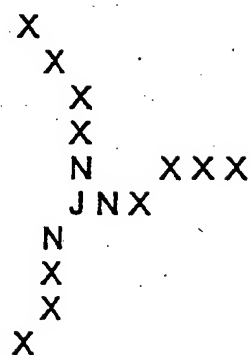


FIG 15A

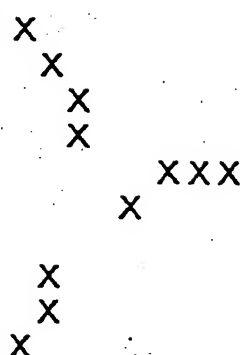


FIG 15B

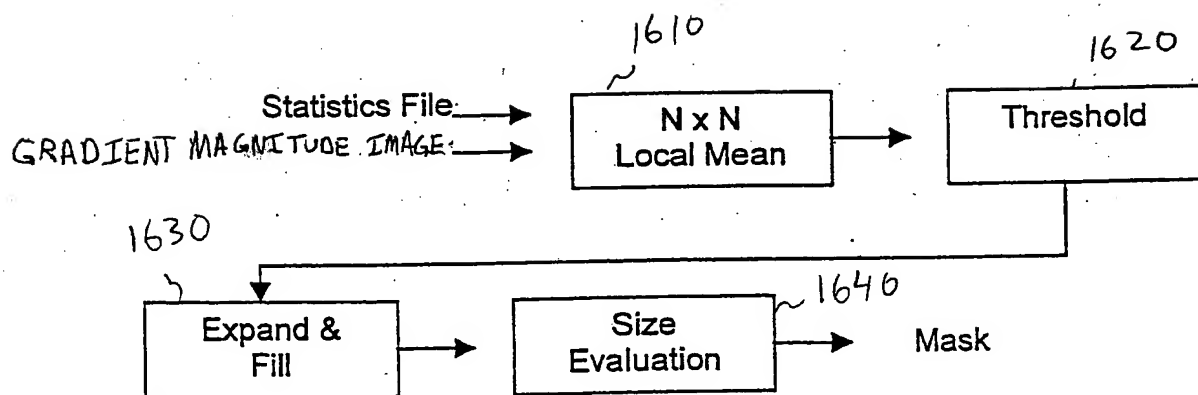


FIG 16

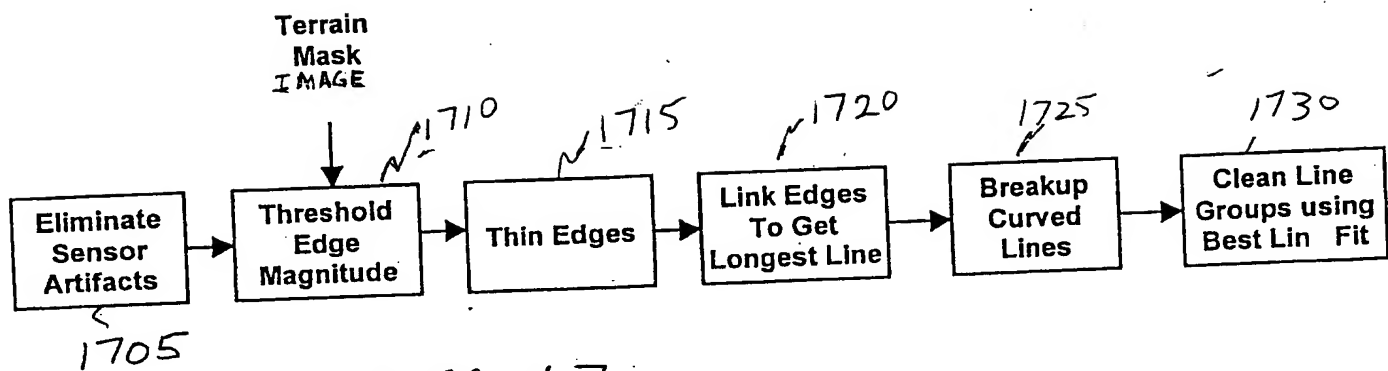
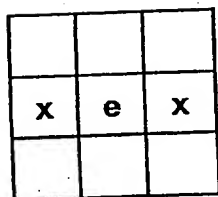
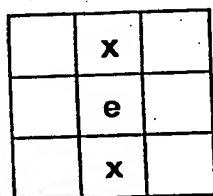


FIG 17



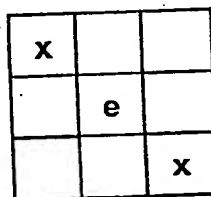
3 and 7

FIG 18A



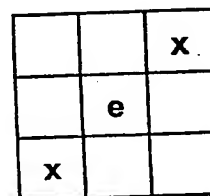
1 and 5

FIG 18B



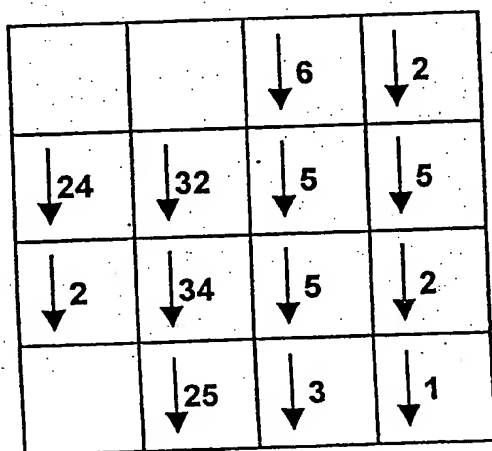
4 and 8

FIG 18C



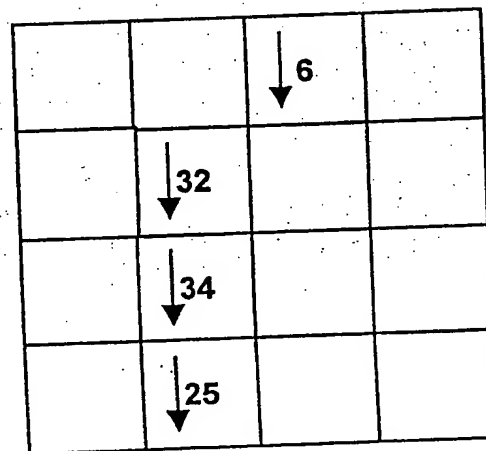
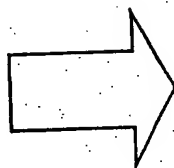
2 and 6

FIG 18D



Edges Directions and Magnitudes

FIG 19A



Thinning Edges

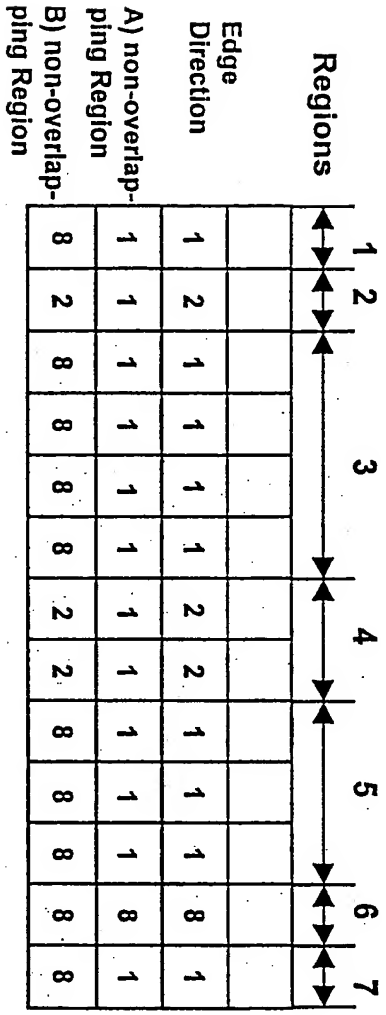
FIG 19B

1	1	1	1	1	1	1			

1	2	1	1	1	1	2	2	1	1

No Noise Present
FIG 26A

Noise Present
FIG 26B



- Direction 1 = direction 1 and direction 2
- Direction 2 = direction 2 and direction 3
- Direction 3 = direction 3 and direction 4
- Direction 4 = direction 4 and direction 5
- Direction 5 = direction 5 and direction 6
- Direction 6 = direction 6 and direction 7
- Direction 7 = direction 7 and direction 8
- Direction 8 = direction 8 and direction 1

FIG 26C



FIG 21A

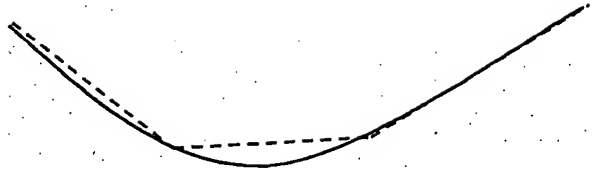


FIG 21B

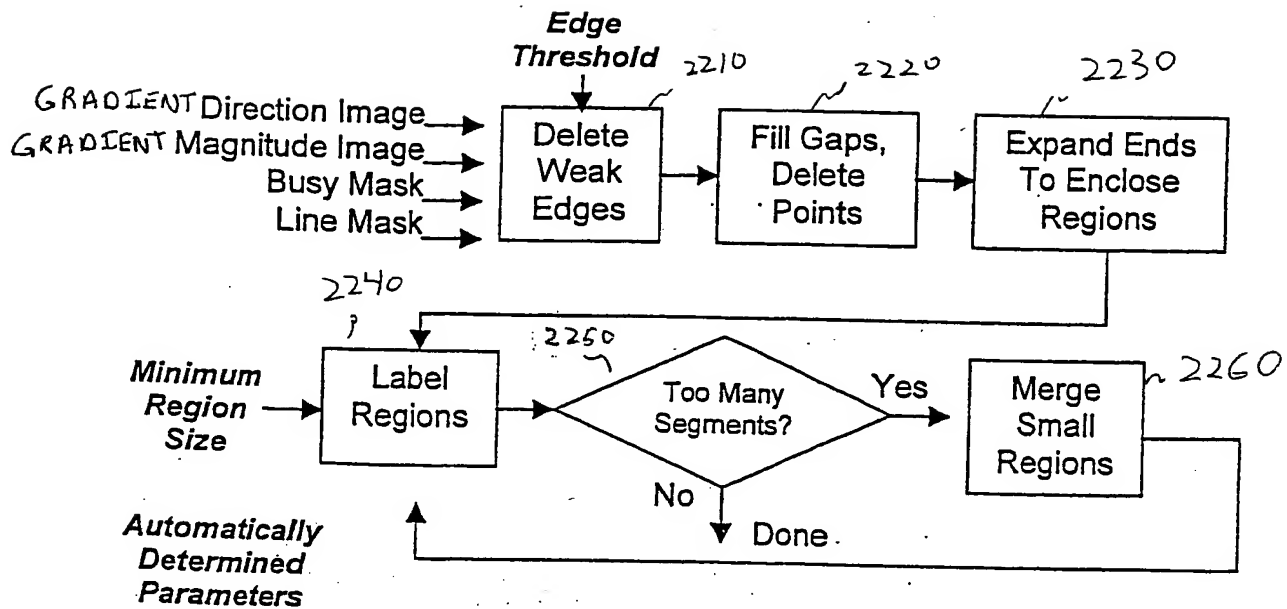


FIG 22

EEO	OEE	OEO	OEO
OCO	OCO	OCO	OCO
OEO	OEO	EEO	OEE

Templates for Vertical Point Gap

C = center pixel, value 1 E = pixel value 1 O = Zero pixel value

EOO	OOE	OOO	OOO
ECE	ECE	ECE	ECE
OOO	OOO	EEO	OOE

Templates for Horizontal Point Gap

FIG 23

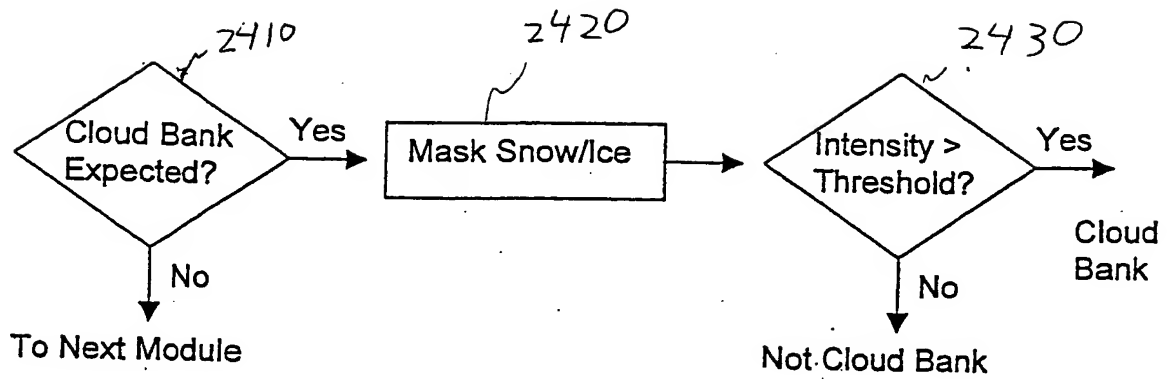


FIG 24

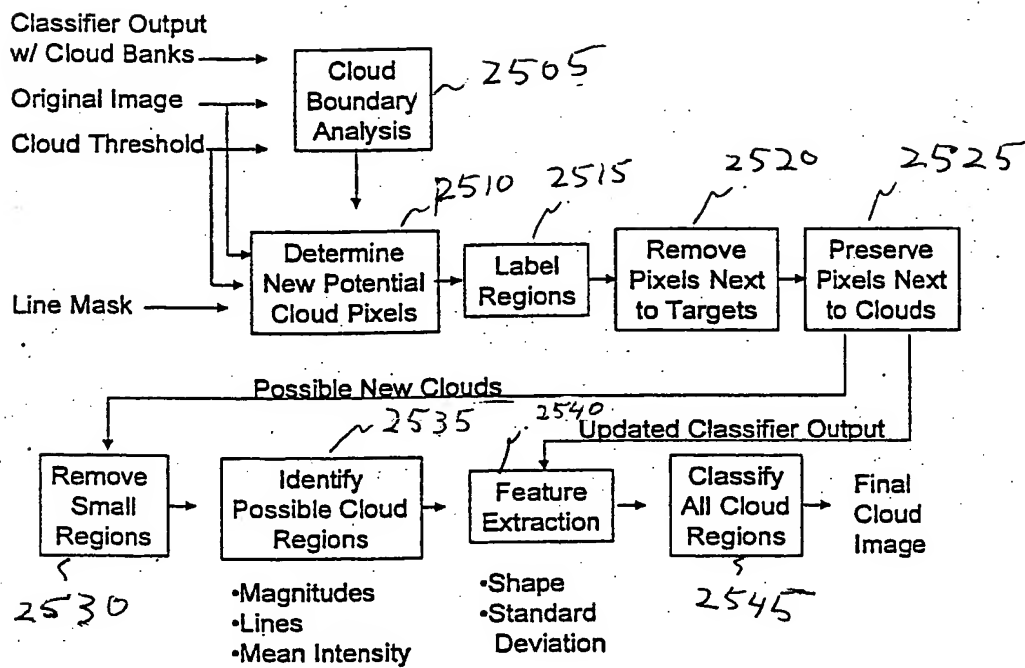


FIG 25

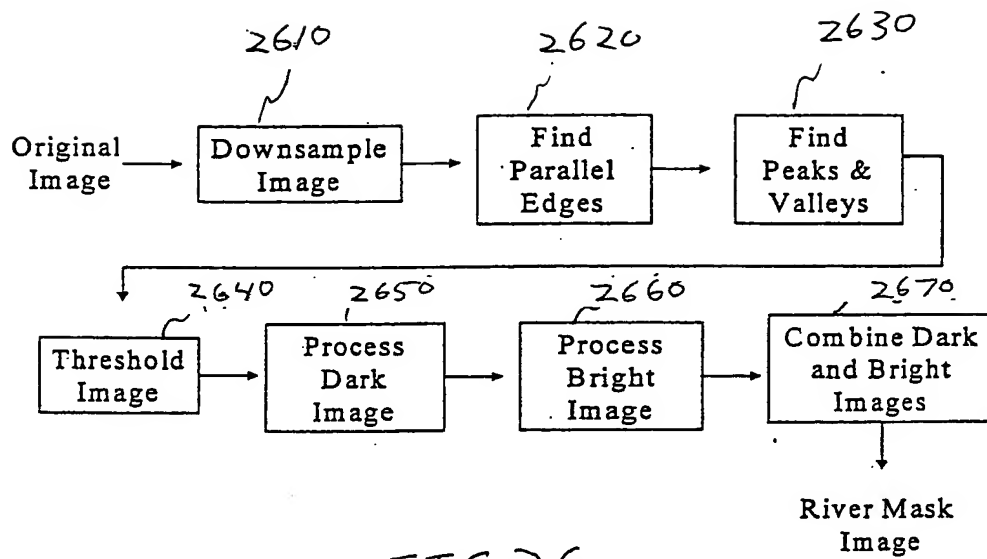


FIG 26

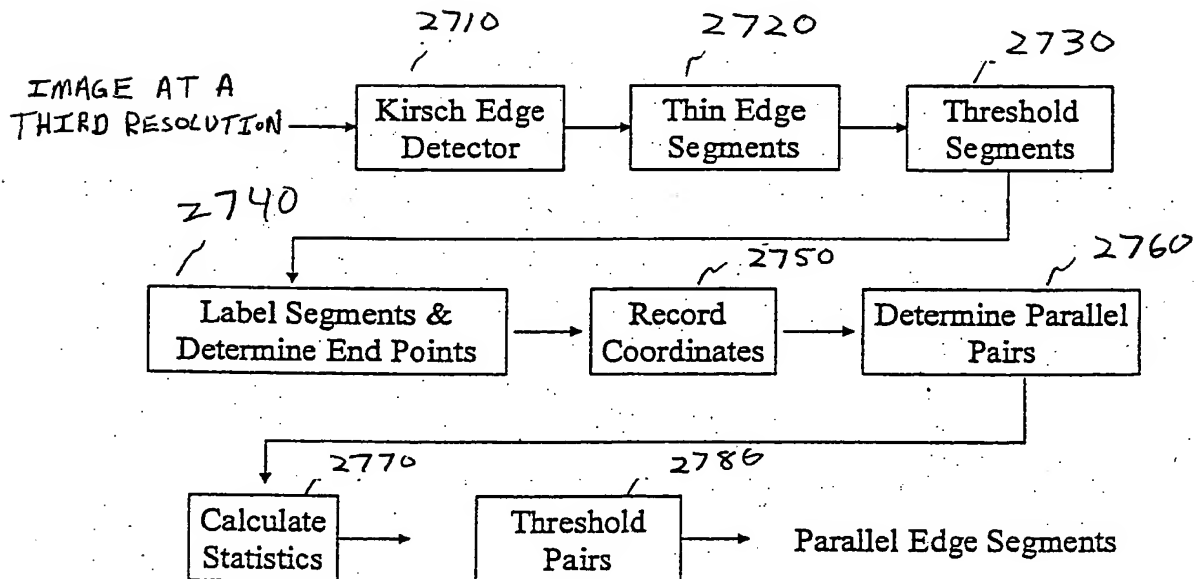


FIG 27

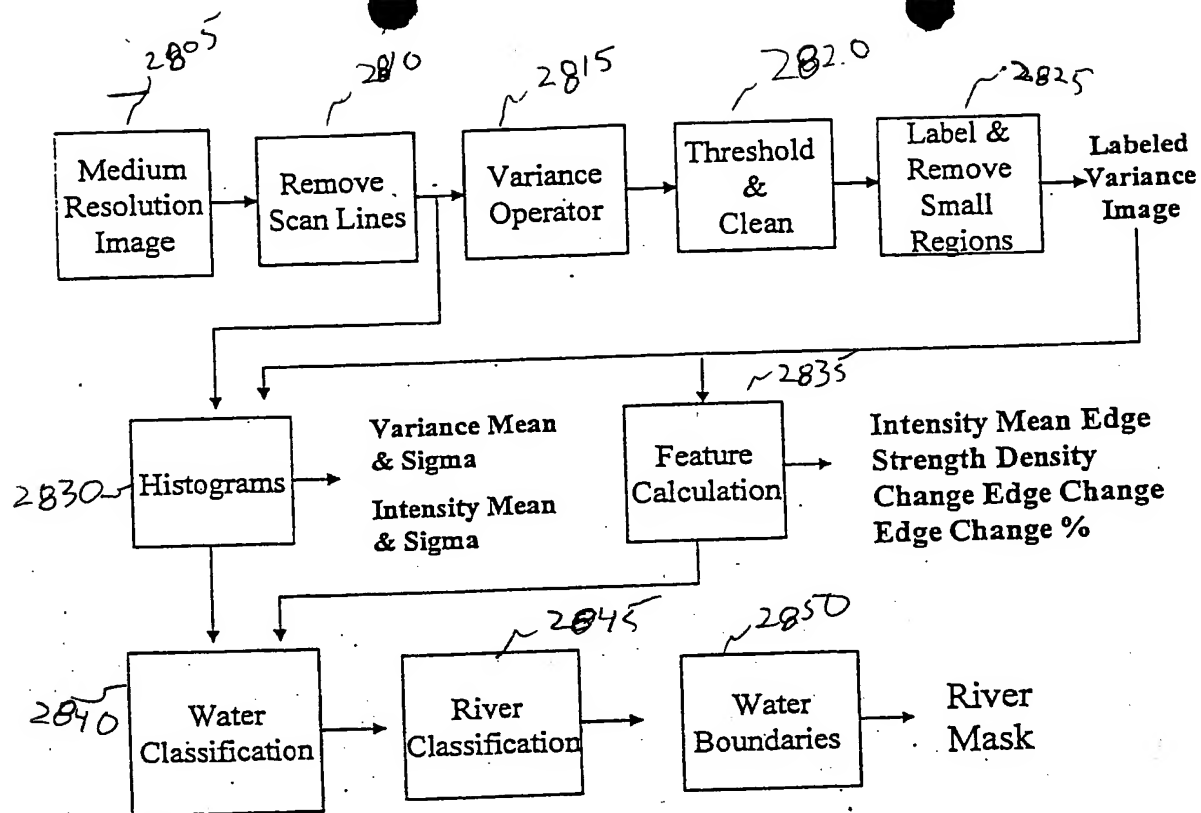


FIG 28

$a_{-1,-1}$	$a_{0,-1}$	$a_{1,-1}$
$a_{-1,0}$	$a_{0,0}$	$a_{1,0}$
$a_{-1,1}$	$a_{0,1}$	$a_{1,1}$

3by3 neighborhood

$$\sigma = \frac{1}{n} \sum_{j=-k}^k \sum_{i=-k}^k (a_{ij} - \mu)^2$$

where

$$\mu = \frac{1}{n} \sum_{i=-k}^k (a_{ij})$$

FIG 29B

For a 3by3 neighborhood $k=1$

FIG 29A

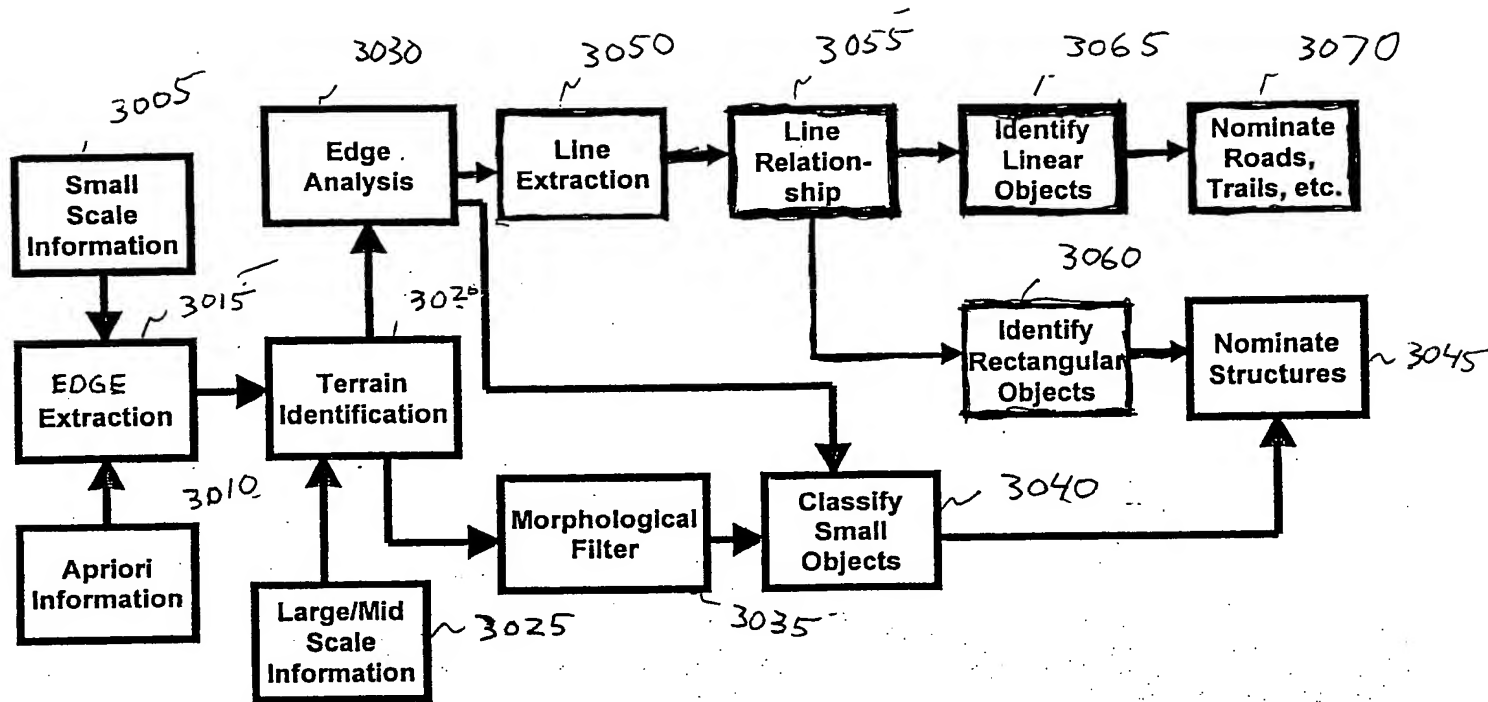


FIG 30

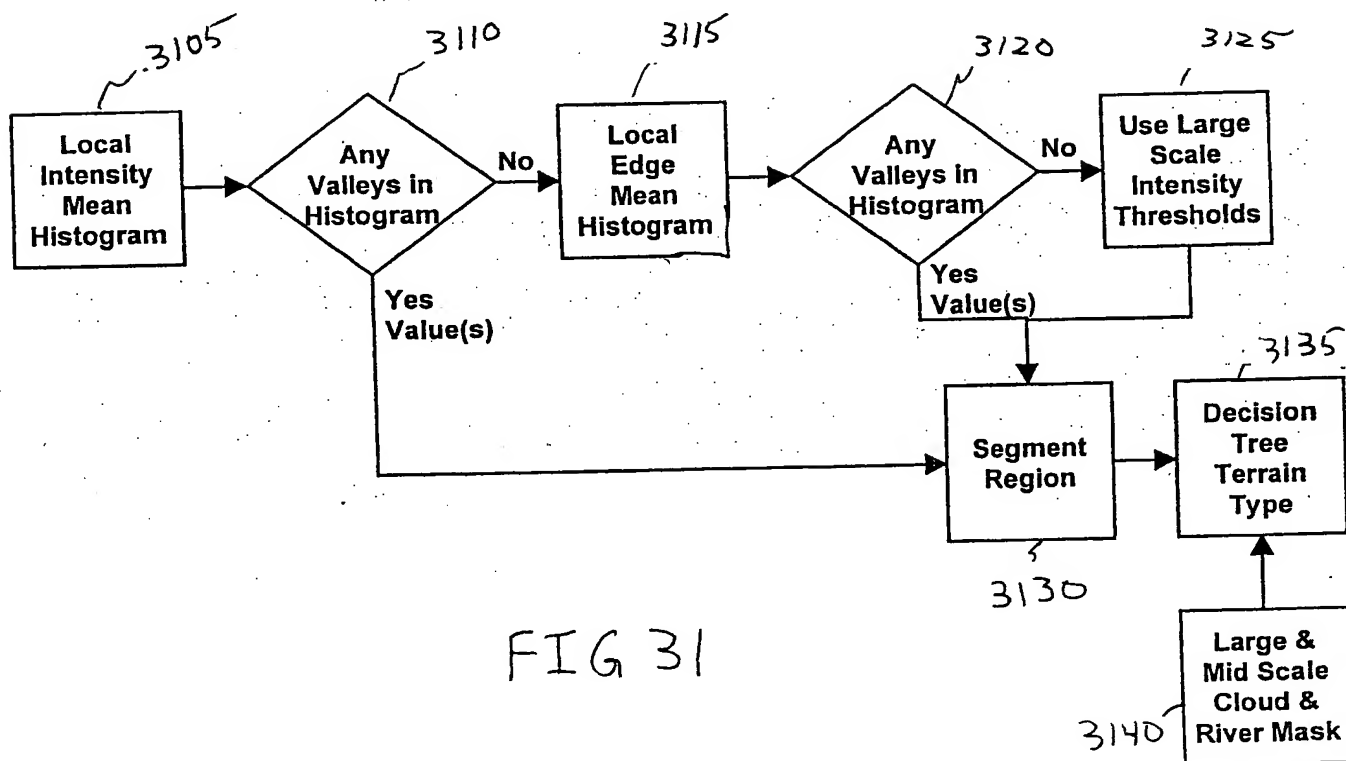


FIG 31

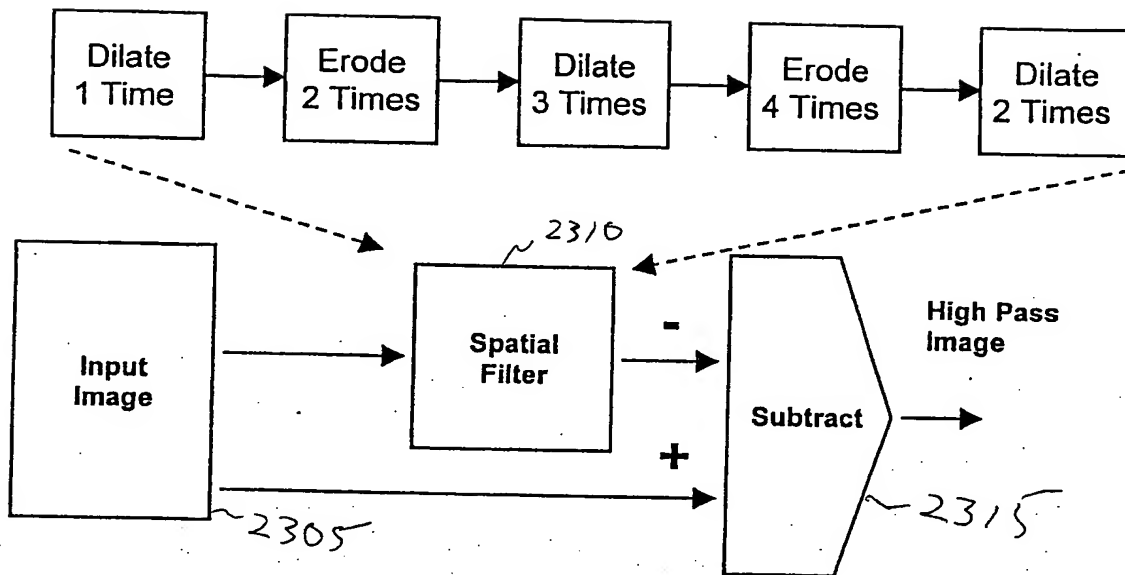


FIG 32

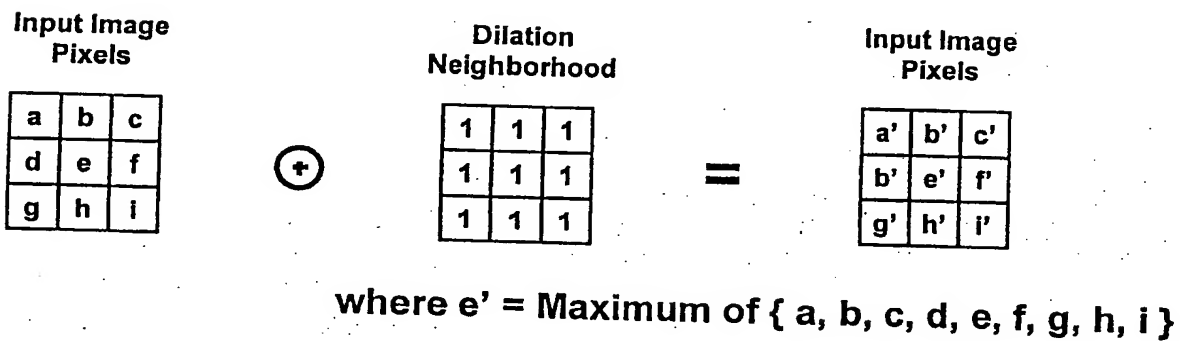


FIG 33A

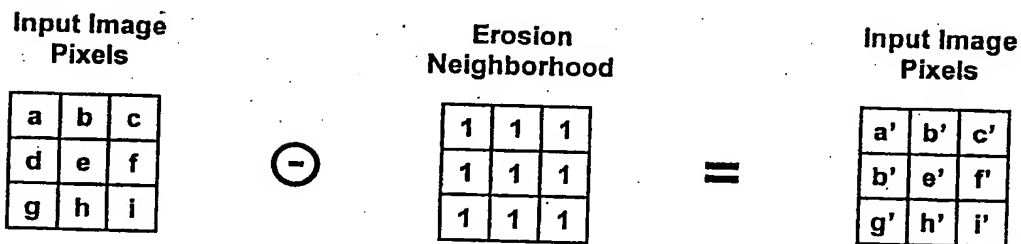


FIG 33B

1 1 1	-1 0 1	0 1 1	-1 -1 0
0 0 0	-1 0 1	-1 0 1	-1 0 1
-1 -1 -1	-1 0 1	-1 -1 0	0 1 1
Horizontal	Vertical	Diagonal 1	Diagonal 2

FIG 34A

	<u>Horizontal</u>	<u>Vertical</u>	<u>Diagonal 1</u>	<u>Diagonal 2</u>
Gradient Sign	+ -	+ -	+ -	+ -
Direction	1 5	3 7	2 6	4 8

FIG 34B

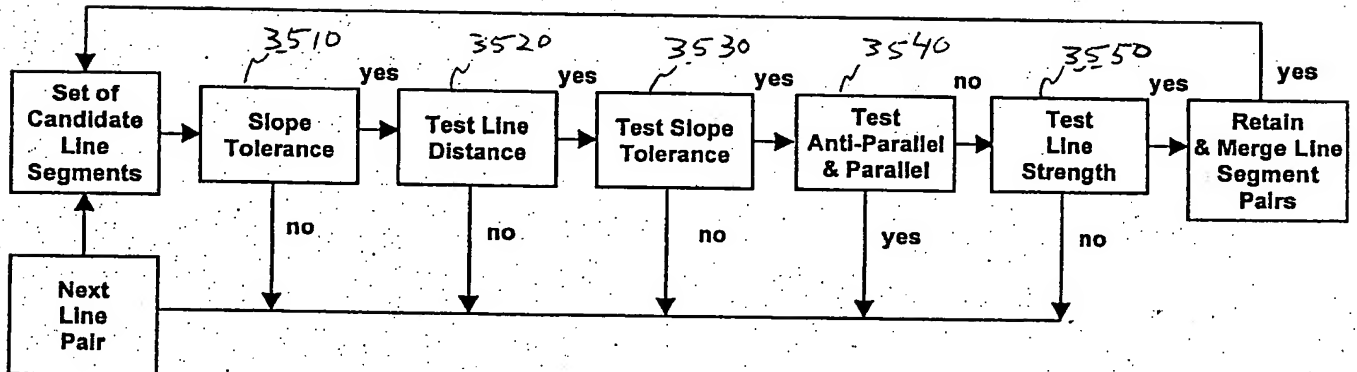


FIG 35

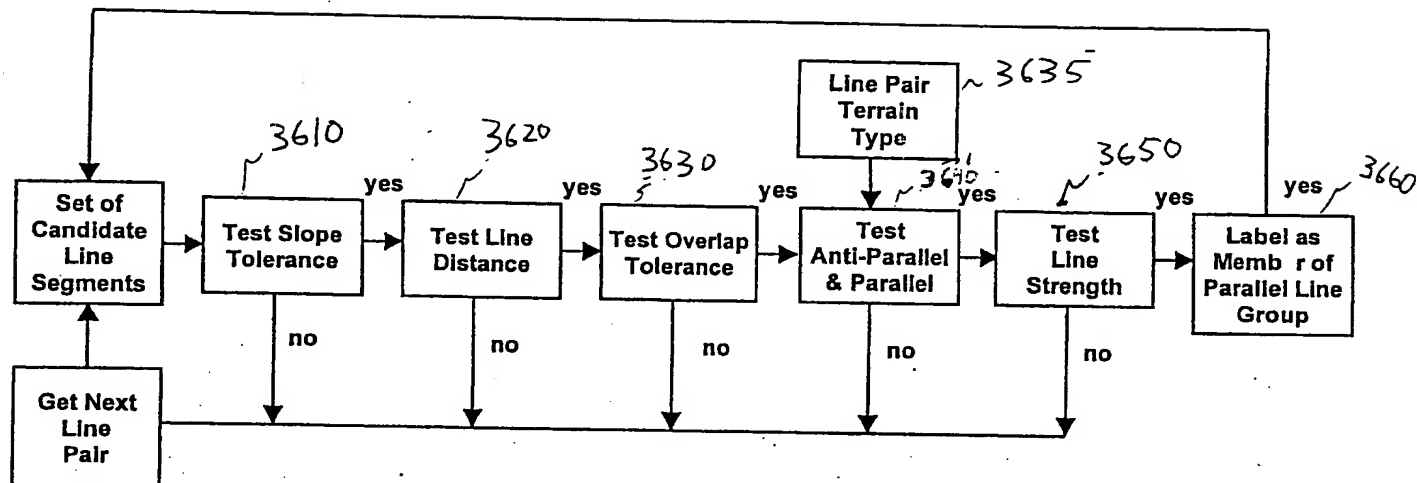


FIG 3.6

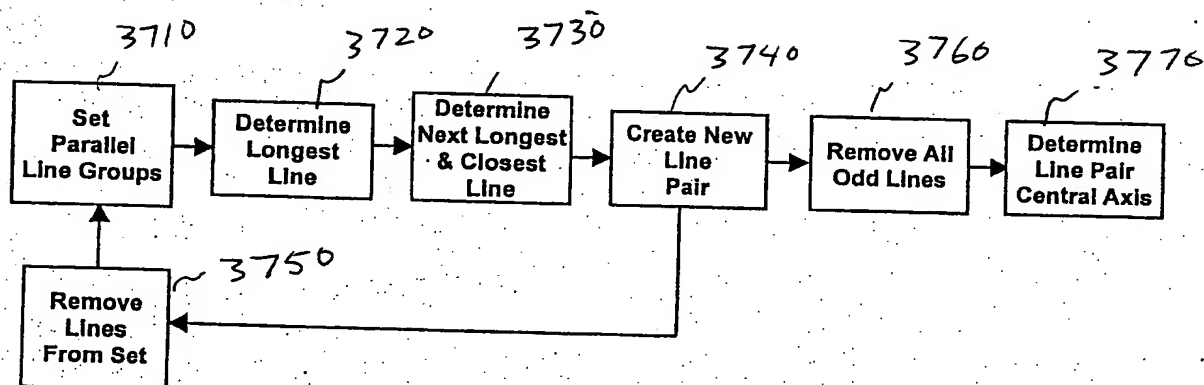


FIG 37

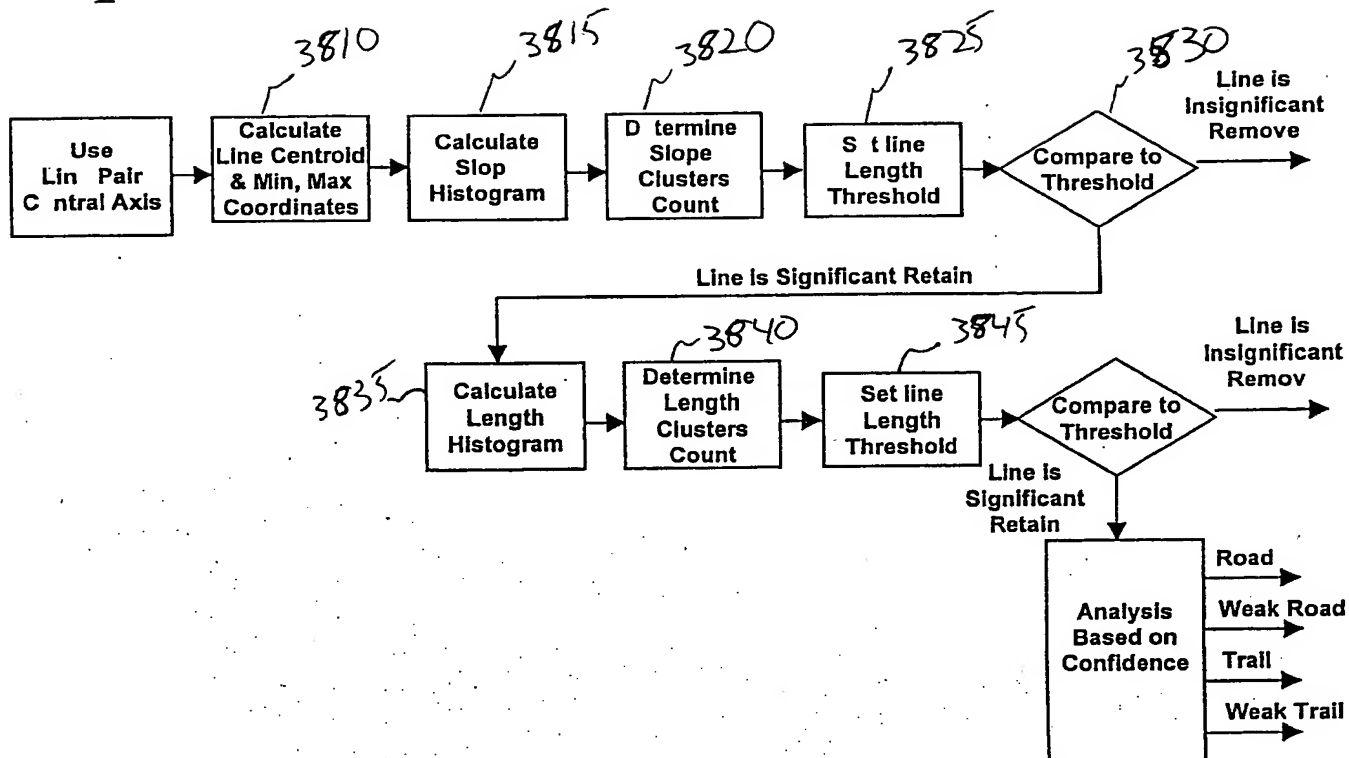


FIG 38

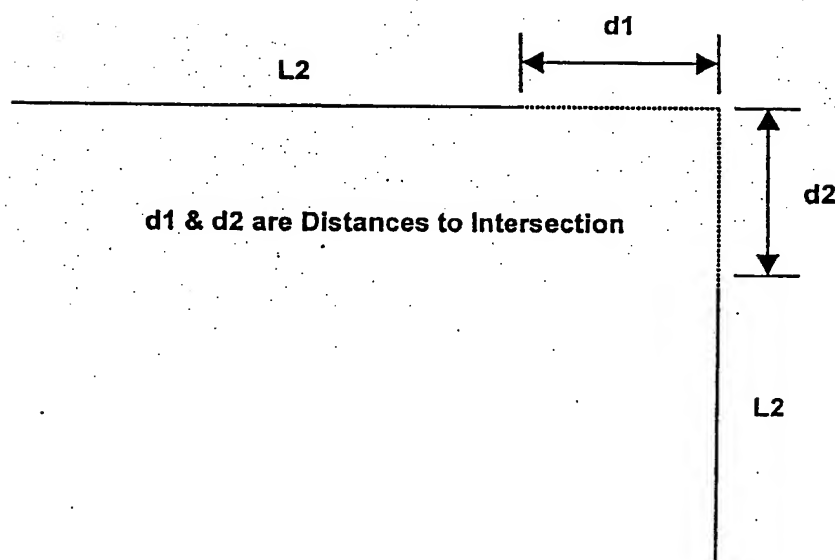
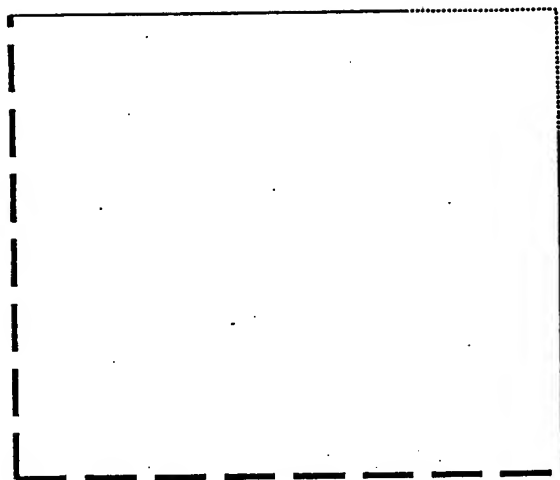


FIG 39



————— Detected Line
 Extended Line
 - - - - - Reflected Line

FIG 40

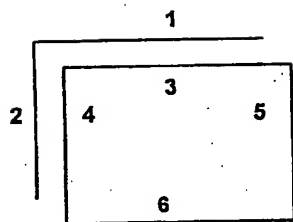


FIG 41A

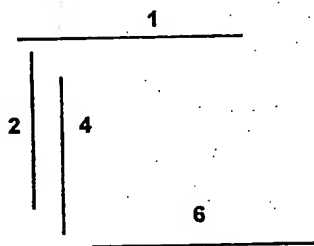


FIG 41B

Reflected and Extended

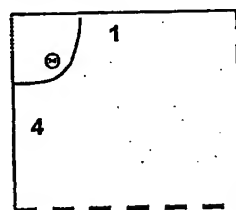


FIG 41C

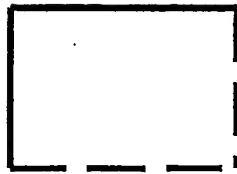


FIG 42A

— Detected Line
 - - - Reflected Line

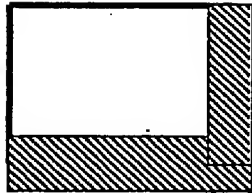


FIG 42B

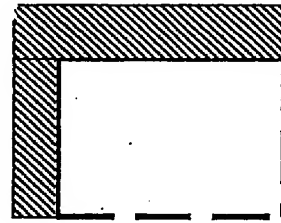


FIG 42C

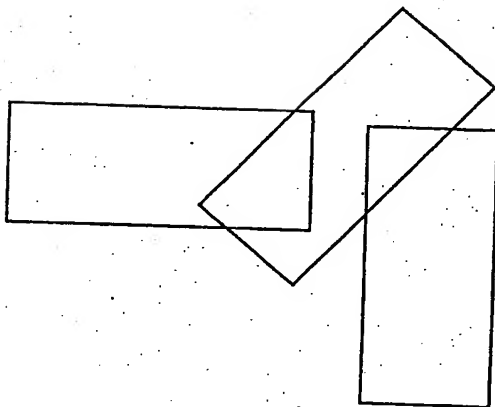


FIG 43A

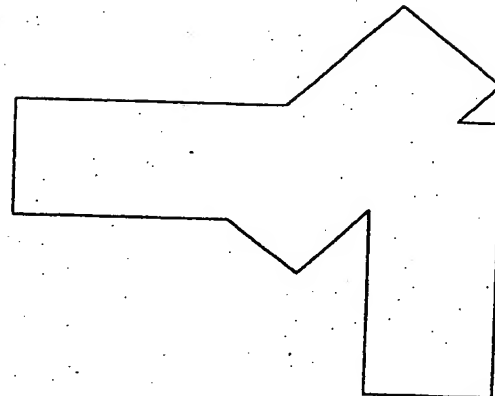


FIG 43B

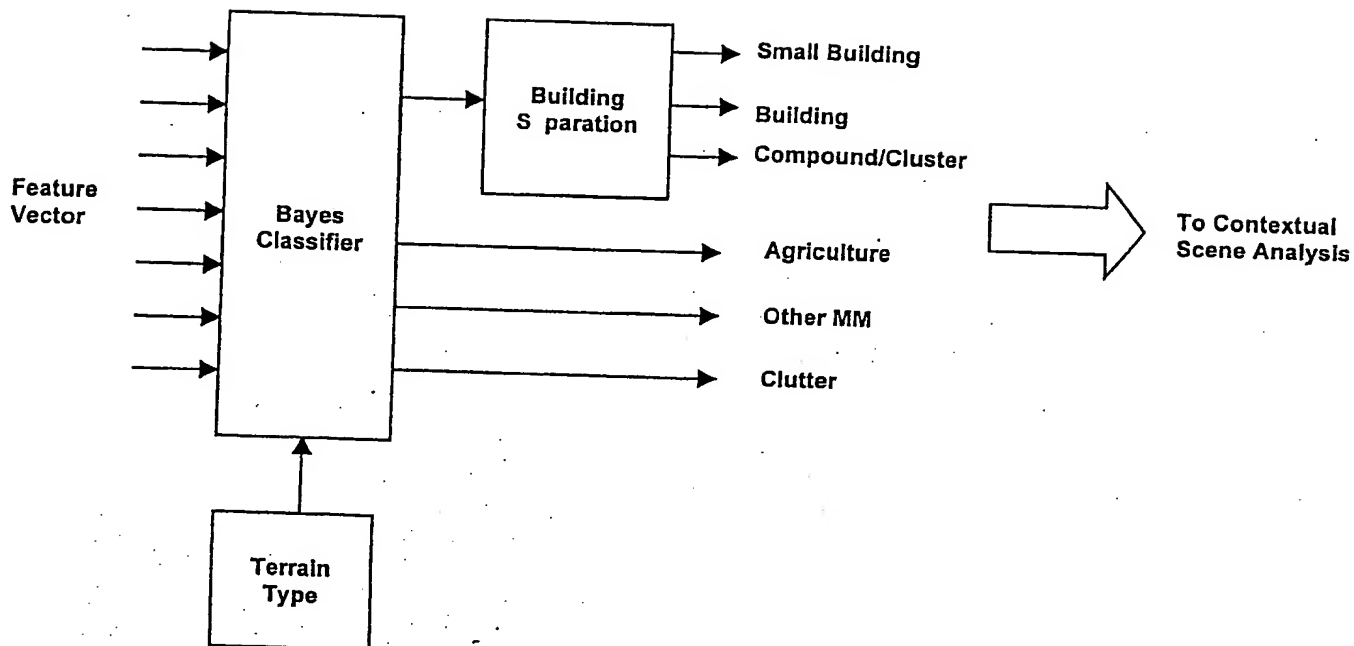


FIG 44

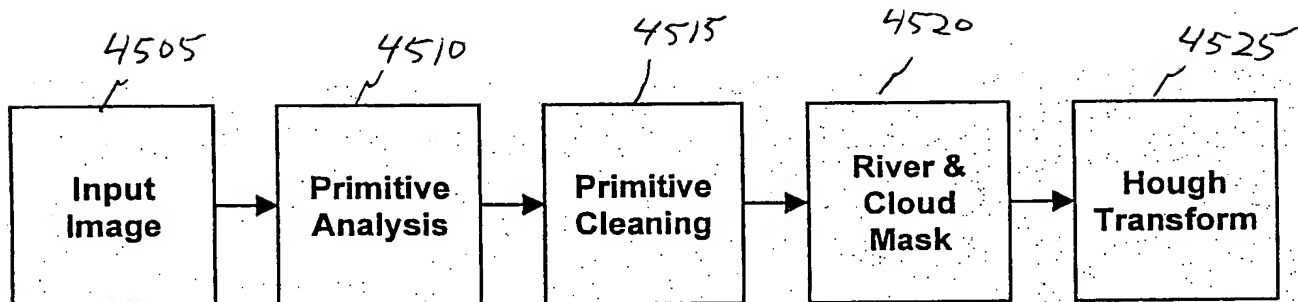


FIG 45

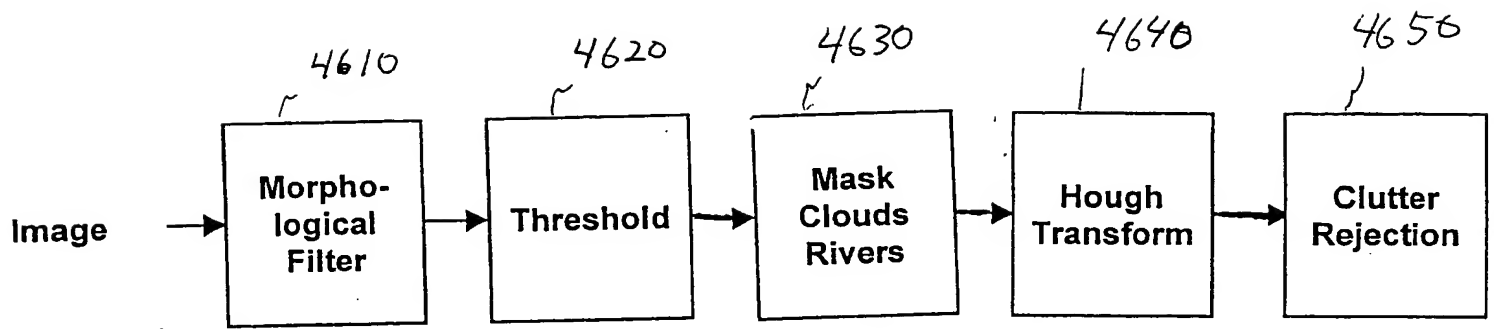


FIG 46

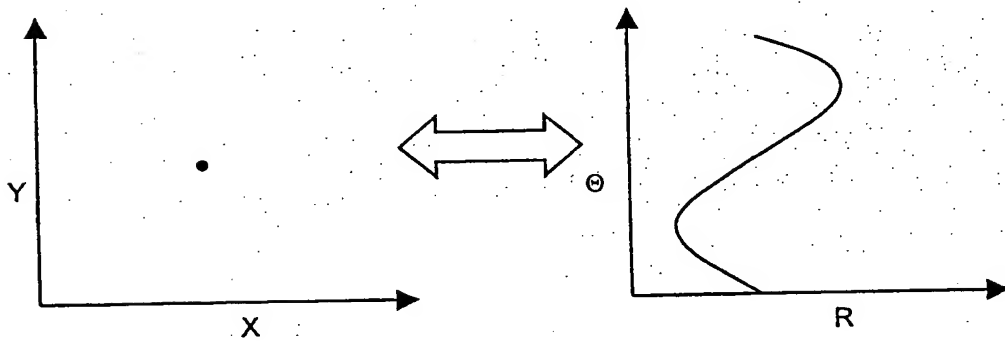


FIG 47A

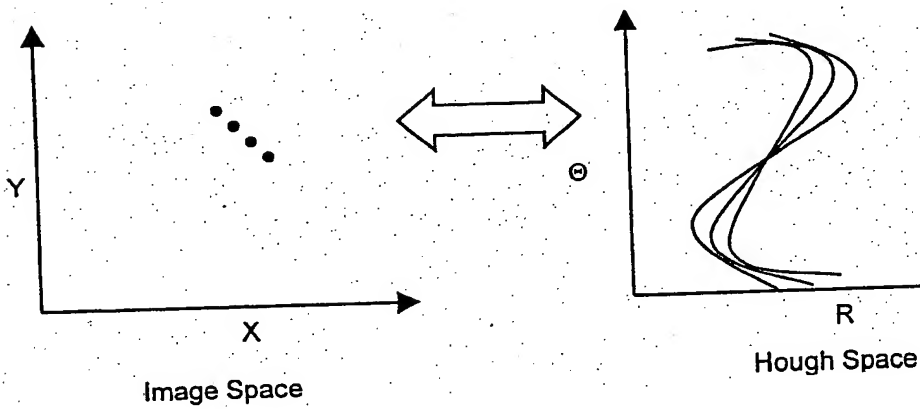


FIG 47B

$$R = x * \cos(\Phi) + y * \sin(\Phi)$$

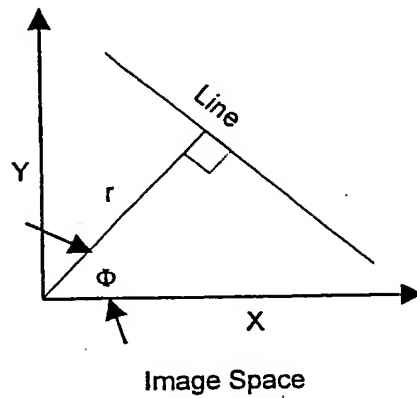


FIG 48

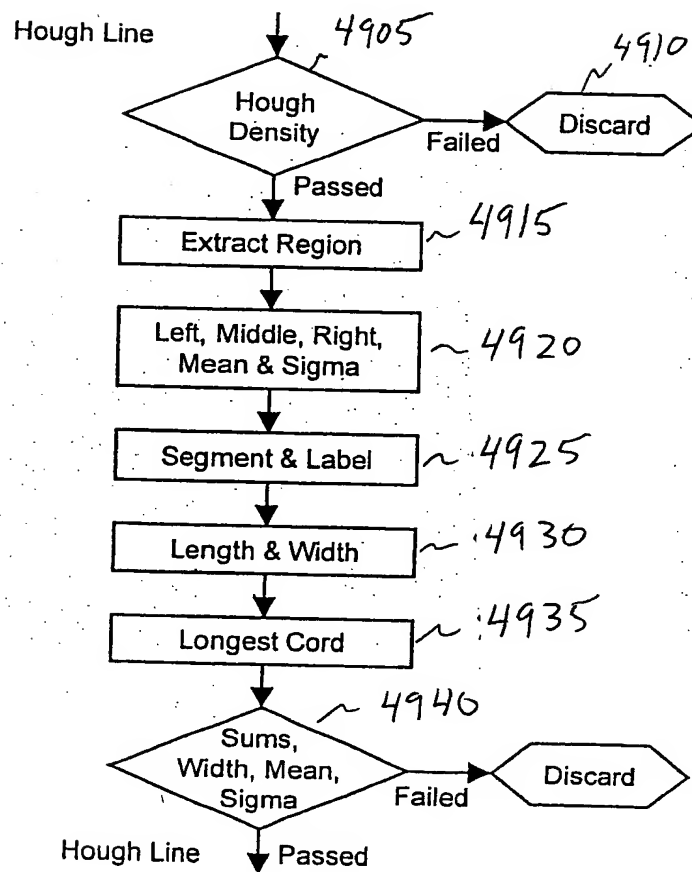


FIG 49

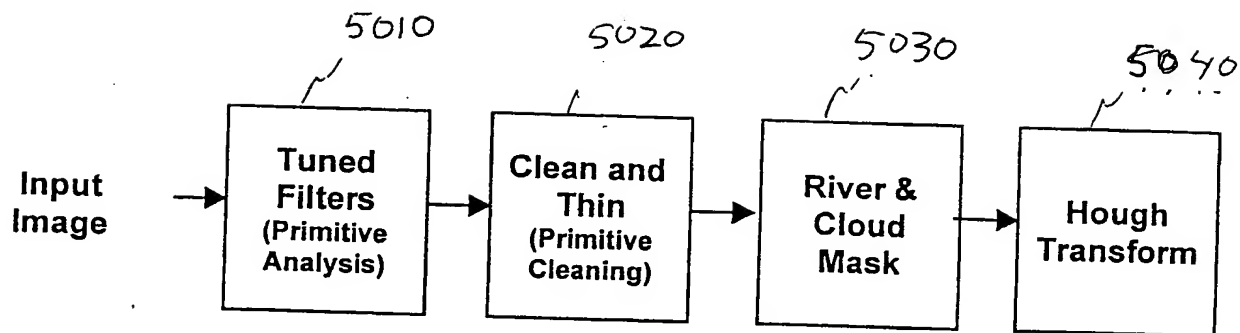


FIG 50

A1	0	B1	0	C1
A2	0	B2	0	C2
A3	0	B3	0	C3
A4	0	B4	0	C4
A5	0	B5	0	C5
A6	0	B6	0	C6
A7	0	B7	0	C7
A8	0	B8	0	C8
A9	0	B9	0	C9
A10	0	B10	0	C10
A11	0	B11	0	C11
A12	0	B12	0	C12
A13	0	B13	0	C13
A14	0	B14	0	C14
A15	0	B15	0	C15

$$B_8 = 2 \times \sum_{i=1}^{15} B_i - \left(\sum_{i=1}^{15} A_i + \sum_{i=1}^{15} C_i \right)$$

FIG 51

A1	A2	A3	A4	A5
A16	B1	B2	B3	A6
A15	B4	B5	B6	A7
A14	B7	B8	B9	A8
A13	A12	A11	A10	A9

FIG 52

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FIG 53

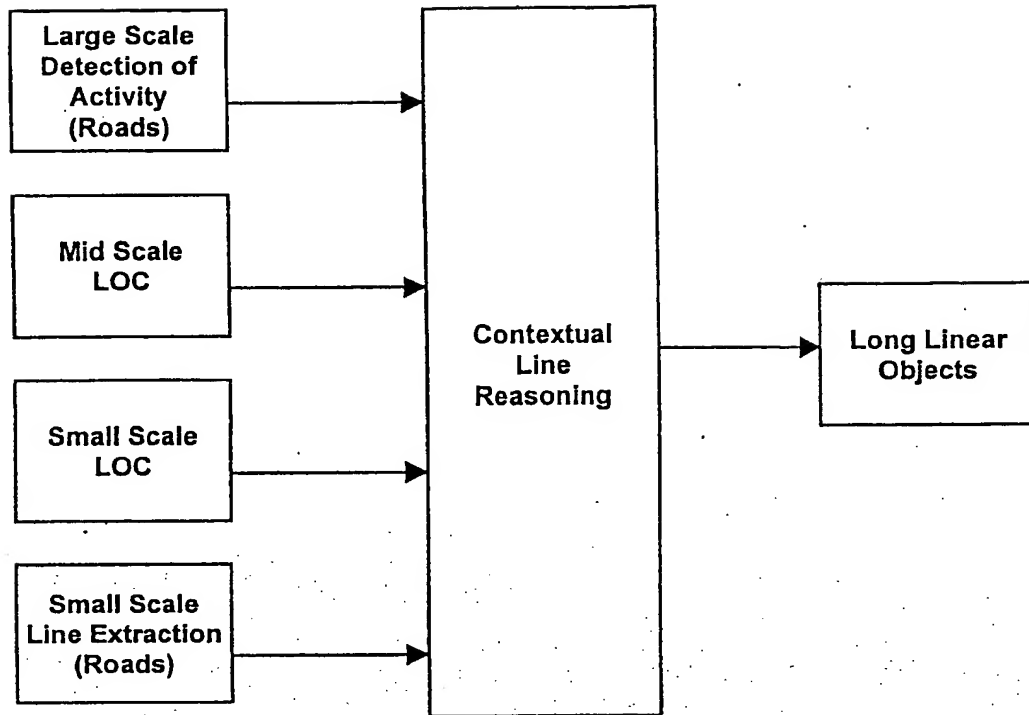


FIG 56

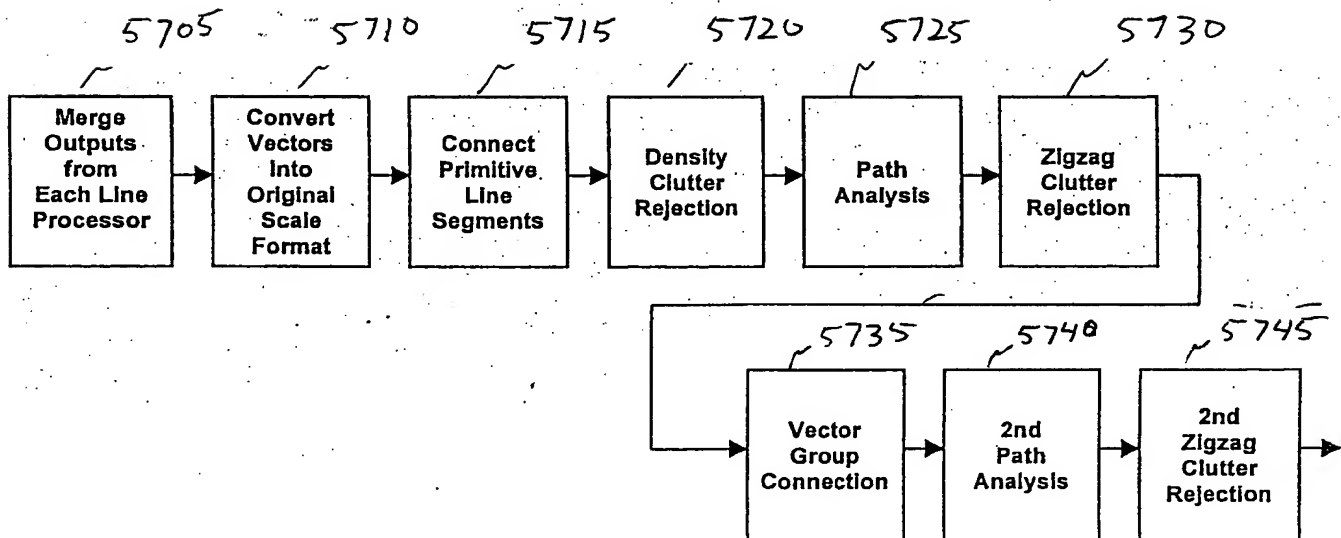


FIG 57

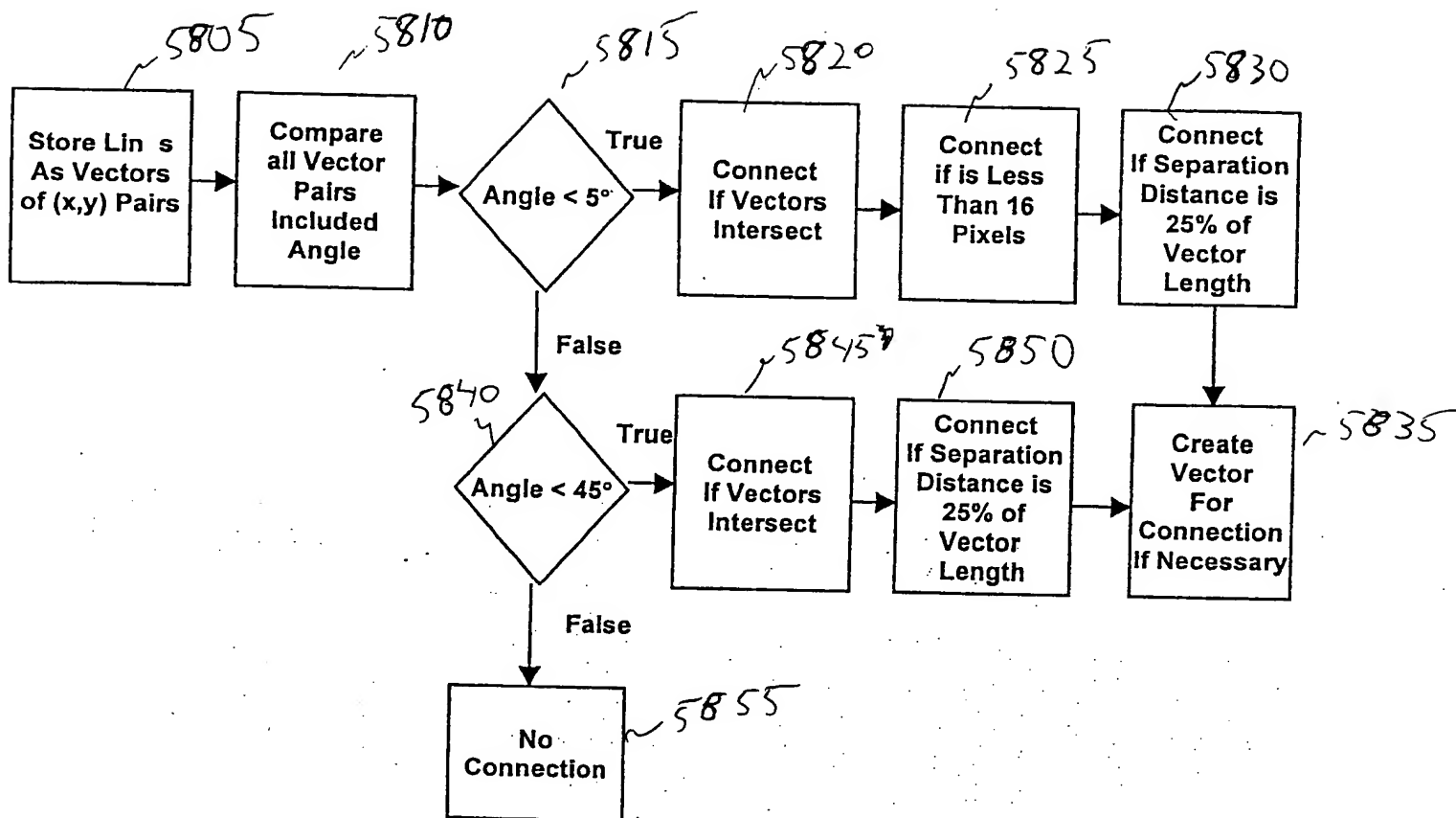


FIG 58

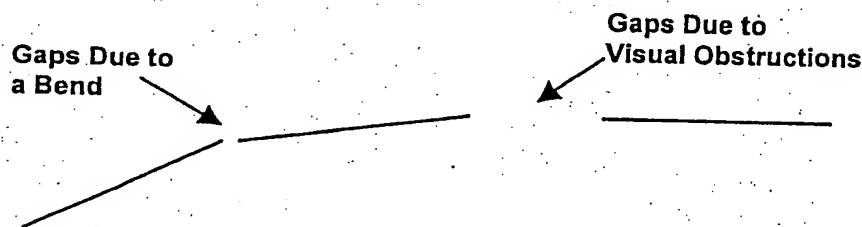


FIG 59A

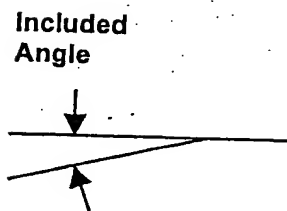


FIG 59B

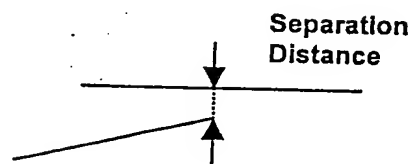


FIG 59C

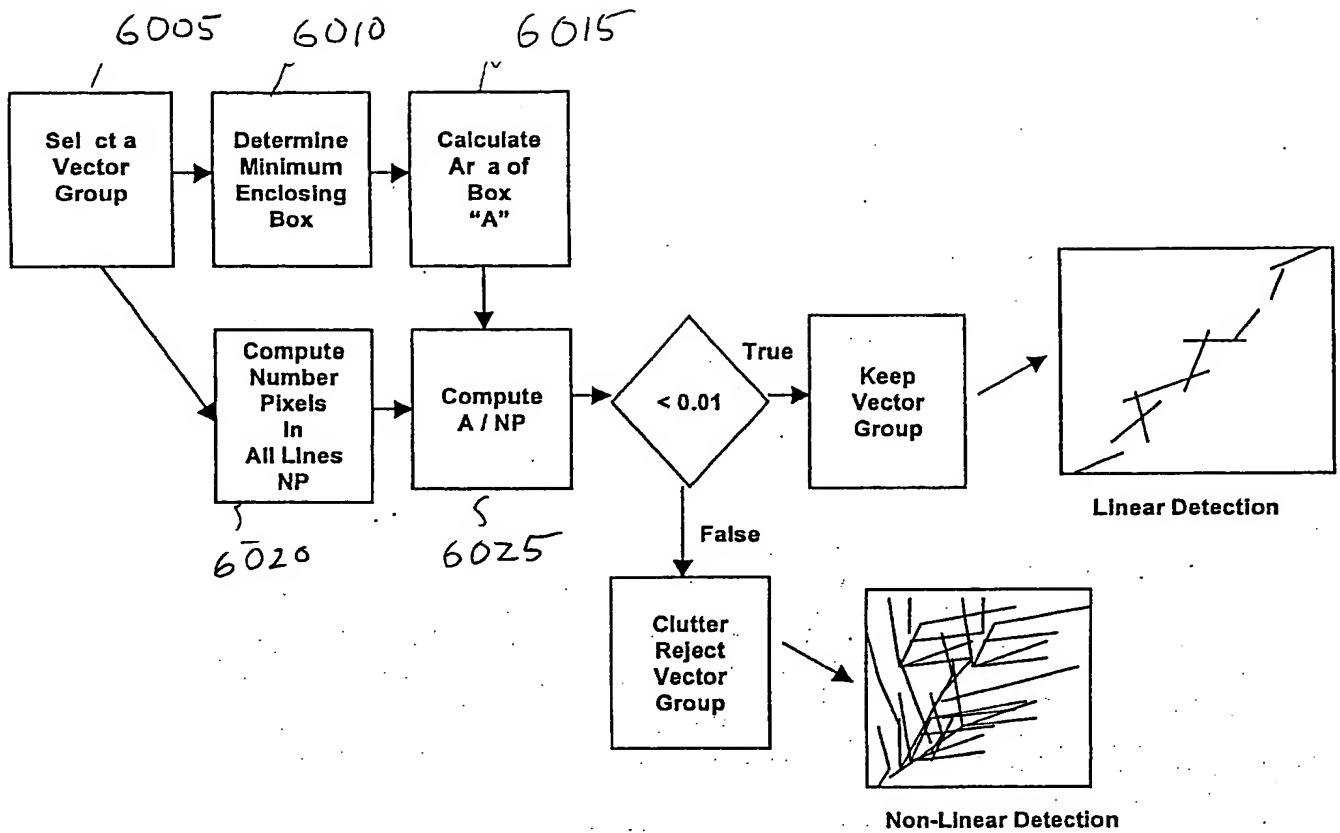


FIG 60

$M^1 = \|m_{ij}^1\|$ Where m_{ij}^1 is the direct distance between node i and j in pixels

$M^2 = \|m_{ij}^2\|$ Where m_{ij}^2 is the direct distance between node i and j in pixels using a most one intermediate node

$$M^2 = M^1 \otimes M^1$$

$$M^4 = M^2 \otimes M^2$$

In general the following is true

$$M^{n+m} = M^n \otimes M^m$$

When $M' \equiv M'^{\alpha}$ where α is a positive number all paths are connect

FIG 61

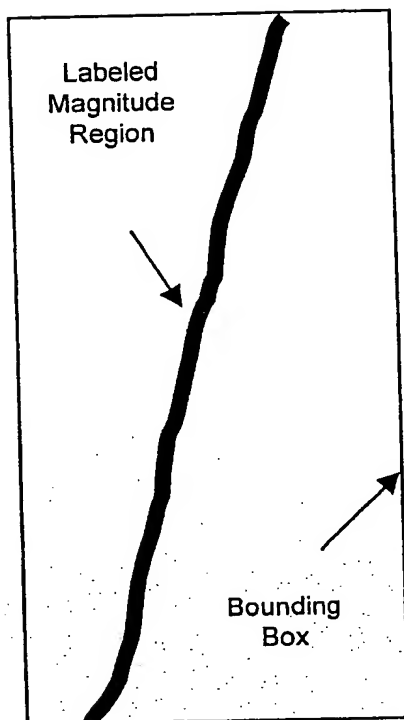


FIG 54

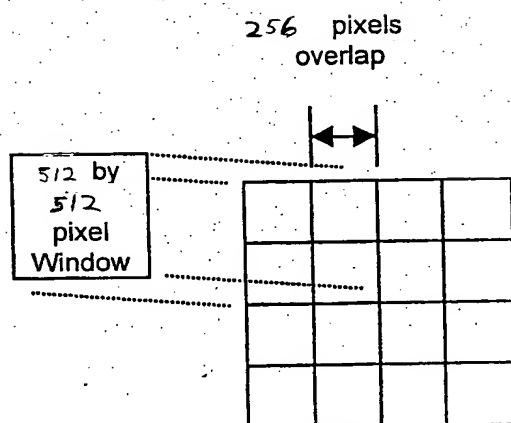


FIG 55

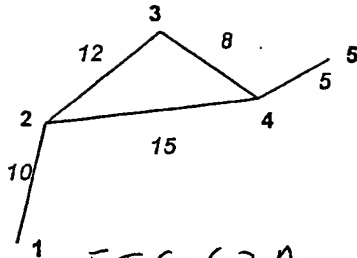


FIG 62A

$$M^1 = \begin{bmatrix} 0 & 10 & 0 & 0 & 0 \\ x & 0 & 12 & 15 & 0 \\ x & x & 0 & 8 & 0 \\ x & x & x & 0 & 5 \\ x & x & x & x & 0 \end{bmatrix}$$

FIG 62B

$$M^2 = \begin{bmatrix} 0 & 10 & 22 & 25 & 0 \\ x & 0 & 12 & 15 & 20 \\ x & x & 0 & 8 & 13 \\ x & x & x & 0 & 5 \\ x & x & x & x & 0 \end{bmatrix}$$

FIG 62C

$$M^3 = \begin{bmatrix} 0 & 10 & 22 & 25 & 30 \\ x & 0 & 12 & 15 & 20 \\ x & x & 0 & 8 & 13 \\ x & x & x & 0 & 5 \\ x & x & x & x & 0 \end{bmatrix}$$

FIG 62D

$$M^3 = M^4$$

FIG 62E

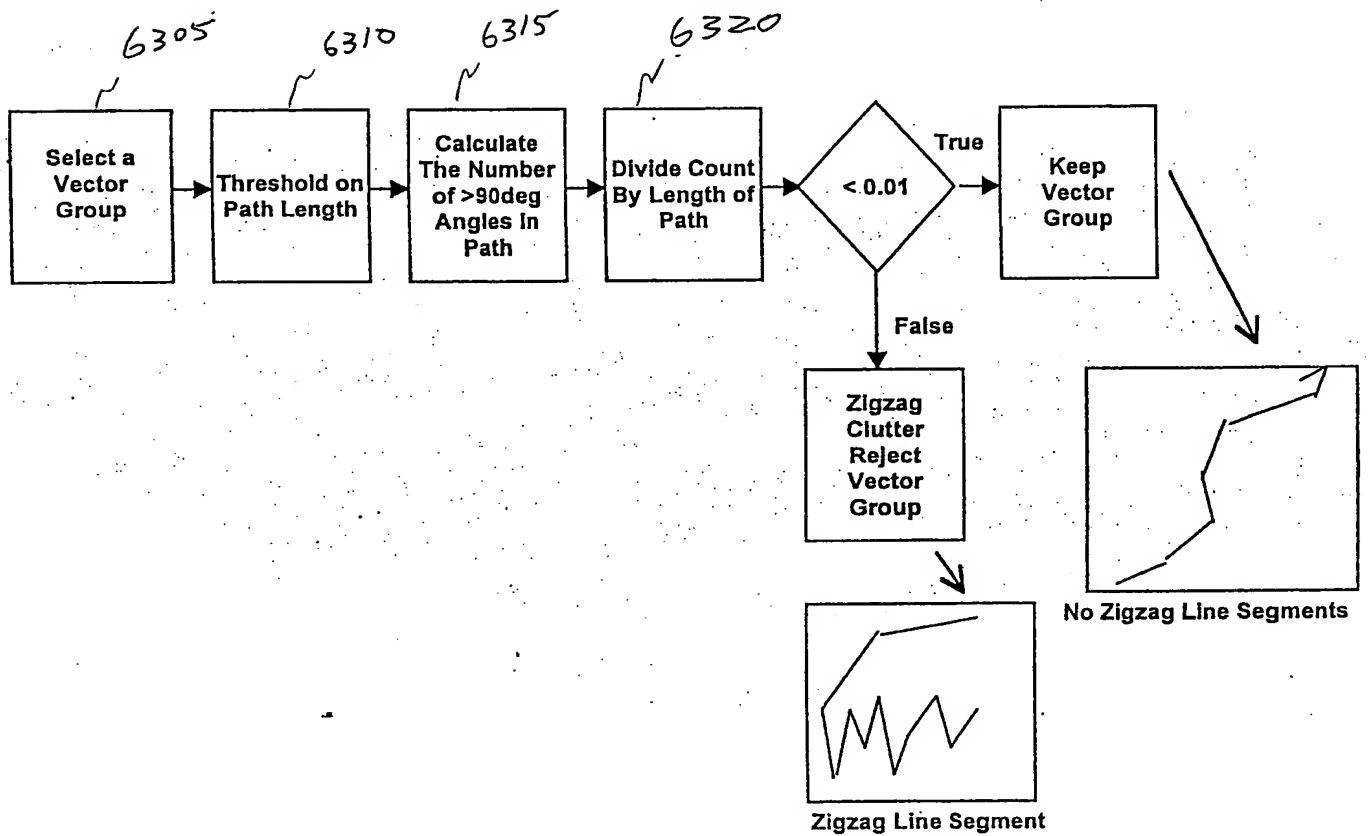


FIG 63

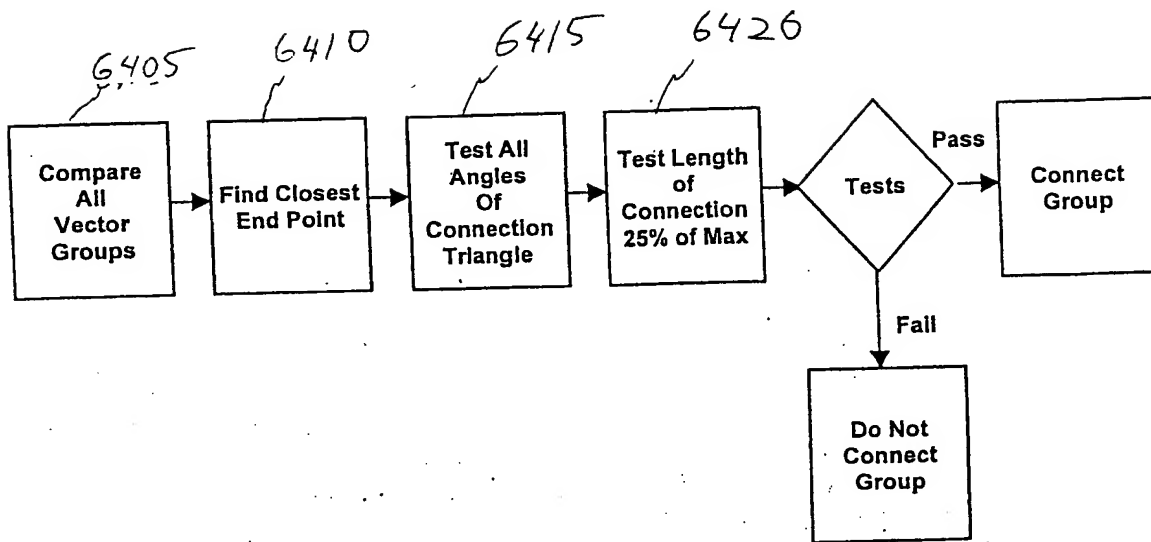


FIG 64

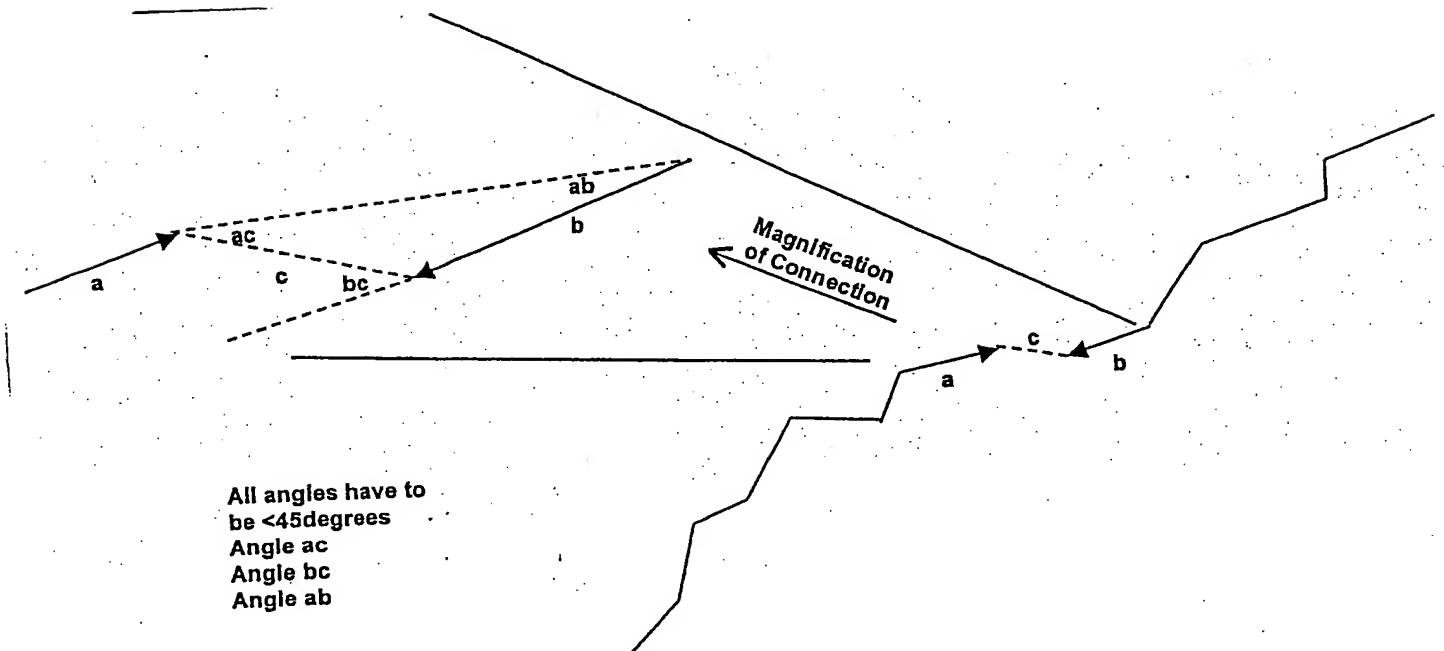


FIG 65

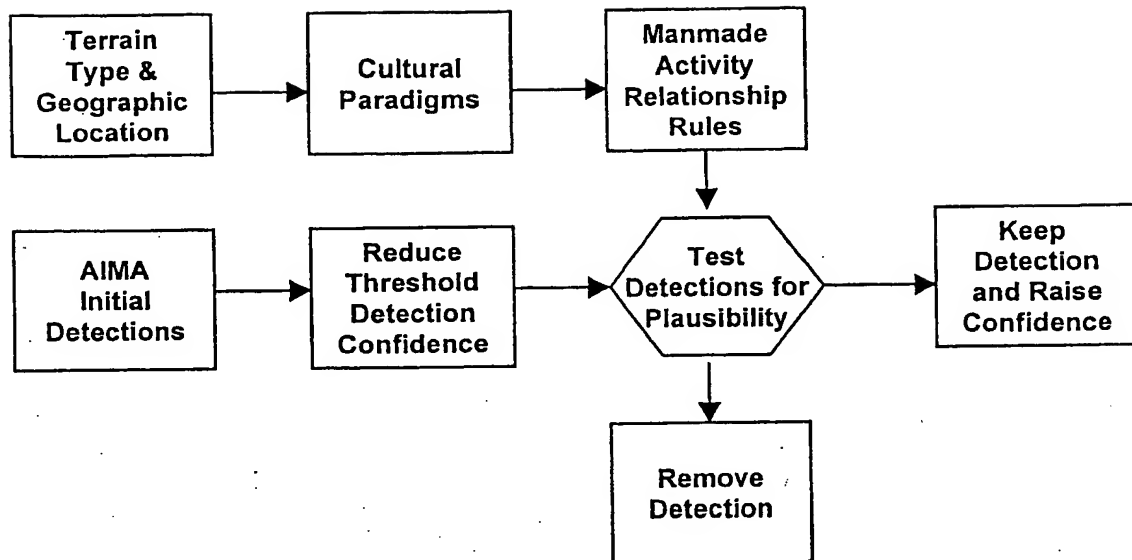


FIG 66